## **Answers to Math 95 Review Sheets Problems**

- 1) z = 25/7
- 2) a)  $y = \frac{3x-8}{2}$  or  $y = \frac{3}{2}x-4$  b)  $x = \frac{7}{r-11}$
- 3) The value of the loom after 5 years is \$1470.
- 4) a) Let *x* be the original price. Equation: (x + 0.40x) - 0.40(x + 0.40x) = 220. Answer: The original price was \$261.90.

Let r be the single discount rate. Equation: 261.90 - 261.90r = 220. Answer: r = 0.16 or 16%

b) Answer: The selling price should be \$95,000.

- 5) ai) 18 ft. aii) 20 sq. ft aiii) 40 cubic ft aiv) 76 sq. ft.
  b) The area of the triangle is 84 sq. in; perimeter 42 in.
  c) Area, approx. 157 sq. cm; Perimeter, approx. 51 cm
- 6) a) For line A: x-int (10, 0), y-int (0, 15)

b) x-int is (2, 0); y-int is (0, -3). c) See graph below.



- 7) a) Slope is 2/5.
  - b) Line A: -3/2, Line B: undefined
  - c) Slope is 0



9) y = -(2/3)x + 6; slope -2/3, y-int (0, 6)

- a) One pair has same slope 4; other pair has slope -1 Slopes 4 and -1 are not negative reciprocals.
  - b) Slope of first is 3/2, the second -2/3. They are negative reciprocals so the lines are perpendicular.
- 11) a) The equation of this vertical line is x = -25.
  - b) A line whose equation is y = -2 is shown above in 6).

12) a) 
$$y-5 = -\frac{1}{5}(x-2)$$
,  $y = -\frac{1}{5}x + \frac{27}{5}$   
b)  $y = -\frac{1}{2}x - \frac{5}{2}$ 

- 13) a) No. For 15 rides, the cost is less without the pass.b) The difference is \$5.
  - c) For 20 rides, the cost will be the same.
  - d) The cost of the pass is \$20.
- 14) ai) Slope is 1 dollar per ride.aii) The cost per ride is \$1 for a person with a pass.aiii) The vertical intercept indicates the pass costs \$20.

b) The vertical intercept is 1549 thousand which says there were 1,549,000 nurses in 1985. The slope is 34 thousand per year which says the number of nurses is increasing at a rate of 34,000 per year.

- 15) (8, 2) No; (2, 0) No; (5, 1) Yes
- 16) a) The solution is x = 8, y = 7, as shown.



b) Solution is x = 5, y = 1, as shown.



- 17) a) The solution is x = 2, y = -3.
  - b) The solution is x = -1, y = -3.
- 18) a) Let x = dollar amount invested in stocks and y = dollar amount in bonds. The system is

 $\begin{array}{l} x + y = 20000 \\ 0.15x + 0.108y = 2496 \end{array}$ 

Answer: \$8,000 in stocks, \$12,000 in bonds

b) 20 gallons of the 30% solution should be mixed with 40 gallons of the 60% solution.

19) a) 
$$9x^4y^{10}$$
 b)  $\frac{5x^7}{16y^5}$  c)  $\frac{b^6}{3a^{11}}$ 

20) 1

- 21) a)  $-12x^4 4x^3 + x^2 + 9x 6$ ; degree 4; leading coefficient -12.
  - b) One possibility is  $5x^6 + 7x^2 9$ .

22) a) 
$$22x^3 - 14x^2 - 4x + 8$$

b) 
$$12x^3 + 4x^2 + 12x - 14$$

23) a) 
$$-10x^5 + 16x^4 - 14x^3 + 6x^2$$
  
b)  $x^3 + 125$   
c)  $35x^2 + 16x - 3$   
d)  $4x^2 - 9$ 

24) a) 
$$1 + \frac{4}{x}$$
 b)  $2x^4 - x + \frac{1}{3x}$ 

25) a) ab(2a-5b+7ab)

b) 
$$(x-3)(7+y)$$

c) 
$$-3x(x-9)$$

26) a)  $(x-3)(x^2+4)$ 

b) 
$$(3x-2)(4x+1)$$

27) a) 
$$(2x-5)(3x+7)$$

- b) 5w(3w-2)(w-1)
- 28) (6x 7y)(6x + 7y)
- 29) a)  $(x-2y)(x^2+2xy+4y^2)$ 
  - b)  $(5b+4)(25b^2-20b+16)$

30) a) 
$$x = 5/2$$
 or  $x = -7/3$ 

b) x = 5/3

- c) x = 0 or x = 4
- 31) a)  $3x^2 x + 5 = 0$  b) 2; 3 c) 5 d) 3, -1, 5
- 32) The fraction is not defined if  $x = \Box 1$  or if  $x = \Box \Box 1$ .

33) a)  $\frac{3}{a+3}$  b) -1/2

34) a) 
$$\frac{5(x+1)}{3}$$
 b) 4  
35) a) 2 b)  $-\frac{1}{2(t-4)}$  c)  $\frac{3x-5}{x(x-5)}$ 

$$36) \qquad \frac{x+4}{x^3}$$

37) a) x = 1/4 b) x = 0 or x = 4

38) About 1053 units should be produced. The average cost cannot be \$4.00 per unit. (Try substituting  $C = \Box 4$  and solve for *x*. What happens?)

39) a) 
$$h(0) = -1$$
,  $h(-4) = 19$ ,  $h(c) = 2c^2 + 3c - 1$ ,  
 $h(5r) = 50r^2 + 15r - 1$ 

b)

F	-13	4	32	212	451
g(F)	-25	-15.6	0	100	232.8

41) a)  $x \le -1$ 

b)  $x \le 10$ ; (- $\infty$ ,10]

b) 
$$x < 18/5$$
 or  $x < 3.6$ ,  $(-\infty, 18/5)$   
42) a) 2 b)  $-1/4$   
43) a) 4.729 b) 34.238, rounded to 3 places  
44) a)  $\Box L^{2/5}m^{4/5}$  b)  $\sqrt[3]{(8x)^2}$  or  $\Box \Box (\sqrt[3]{8x})^2$   
45) ai) 6 aii) 25 aiii) 27 b)  $14y^{7/12}$   
46) a)  $2x^2y^2\sqrt{11y}$  b)  $4x^6\sqrt{2x}$   
47) a)  $3x$  b)  $\Box \frac{x^2\sqrt{2x}}{3}$   
48) a)  $\frac{\sqrt{2}}{2}$  b)  $\frac{\sqrt{30}}{6}$    
49)  $-2\sqrt{3}$    
50) a)  $10\sqrt{3} + 2\sqrt{6}$  b)  $\sqrt{6} + \sqrt{10} + \sqrt{21} + \sqrt{35}$    
51) a)  $x \Box = 9$  b)  $x \Box = 3$  or  $x = -1$ 

c)  $x \square = \square -2$  or  $x = \square - \square 4$ 

- 52) The speed was approximately 30 mph.
- 53)  $3i\sqrt{5}$
- 54) a)  $x = \pm \sqrt{8}$  or  $\pm 2\sqrt{2}$ b)  $y = \frac{1 \pm 4}{3}$ , thus y = 5/3 or y = -1
- 55) a)  $x = \pm 4i$  b)  $x = \frac{3 \pm 2i}{2}$  or  $\frac{3}{2} \pm i$
- 56)  $(x+3)^2 = 14$ , thus  $x = -3 \pm \sqrt{14}$
- 57) √<u>101</u>
- 58) a)□ Discriminant is 44; there will be two real solutions.
   b□) Discriminant is □-76; there will be two imaginary solutions.

59) a) 
$$x = \frac{-6 \pm \sqrt{44}}{-4}$$
 which when simplified,  $x = \frac{3 \pm \sqrt{11}}{2}$   
b)  $t = -3 + 2i$  or  $t = -3 - 2i$ 

- 60) a) x = 3 or x = 9 b)  $x = 4 \pm \sqrt{5}$
- 61) a) The dimensions are  $10\sqrt{5}$  by  $20\sqrt{5}$ , or approximately 22.4 feet by 44.7 feet.
  - b) The base is 16.3 inches; the height is 12.3 inches.





- 63) The solutions are the *x*-intercepts of the graph,  $x \approx -1.5$  and  $x \approx 3.5$ .
- 64) a) parabola b) symmetry c) (1, -6) d) minimum
- 65) a) Opens upward b) Opens downward
- 66) y-int (0, -5); x-intercepts: (1.35, 0) and (-1.85, 0)
- 67) x = 1 is the equation of the axis of symmetry. The vertex is located at (1, -9).



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- 69) The parabola opens upward and therefore has a minimum point at the vertex, (3, −32).
- 70) a) The maximum height was 105 feet.
  - b) It took 2.5 seconds to reach that height.
  - c) It hits the ground 5 seconds after launch.
  - d) When t = 0, h = 5. So the *y*-int is 5 feet and this is the height of the platform.
- 71) f(-1) = 5/2, f(3) = 40
- 72) a) The account giving 5.6% compounded semiannually will grow to \$7908.28; 5.3% monthly yields \$7816.02. Thus, the first is better by \$98.26.
  - b) For continuous compounding, the balance will be \$7820.58, for a total interest of \$1820.58.
  - c) There were approximately 1200 people in 1970. In 2010, 40 years later, the predicted population is about 2260.
- 73) a)  $2^6 = 64$  b)  $10^B = A$  c)  $e^{3.5} = x$ d)  $\log_3 81 = 4$  and  $x = \ln 100$ 
  - e)  $\log_5 125 = 3$  because 3 is the exponent on 5 to get 125
  - f) The exponent on 2 is 1.7 because  $2^{1.7} = T$ .
- 74) 0.3522 ; 2.3522 ; 1.9544 ; 6.5596 ; log (-40) does not exist